

# (Super)rare decays of an extra $Z'$ boson via Higgs boson emission

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## Abstract

The phenomenological model of an extra U(1) neutral gauge  $Z'$  boson coupled to heavy quarks is presented. In particular, we discuss the probability for a light  $Z_2$  mass eigenstate decay into a bound state composed of heavy quarks via Higgs boson emission.

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1. Theoretical interest in an extra neutral vector boson  $Z'$  is mainly motivated by experimental observation of possible deviations from the Standard Model (SM) predictions for the decay of the SM  $Z$  boson into  $\bar{c}c$ - and  $\bar{b}b$ - pairs of quarks ( $R_c$ - and  $R_b$ -ratios) [1]. The deviations may be considered as one of the indications of new physics (NP) beyond the SM. The promising explanation of the observed phenomena is implied in the extra  $Z'$  models (see refs. [7-16] in [2]). New gauge bosons can be detected in future high-energy colliders, namely, Large Hadron Collider (LHC) at CERN, which can test the nature and structure of many theoretical models at a scale of 1 TeV, at least. Theoretical predictions of new neutral or charged gauge bosons come from various extensions of the SM [3]. New extra bosons naturally appear in the Grand Unification Theory (GUT) models [3]. A simple and well-known version among the extensions of the SM is the minimal one, aimed at unifying interactions, the  $E_6$  GUT model [3]. Since the breaking of  $E_6$  GUT into SM is accompanied by at least one extra U(1) group

$(E_6 \rightarrow SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1))$ , there may exist a heavy neutral boson  $Z'$  which can mix with an ordinary  $Z$  boson. There are two new gauge bosons appearing in  $E_6$  GUT models [3] where only one originates from the  $SO(10)$  subgroup

$$\begin{aligned} E_6 &\supset SO(10) \times U(1)_\Psi , \\ SO(10) &\supset SU(5) \times U(1)_\chi , \\ SU(5) &\supset SU(3)_C \times SU(2)_L \times U(1)_Y , \end{aligned}$$

while the  $Z'$  boson is a composition of  $Z_\Psi$ - and  $Z_\chi$ - components mixed with a free angle  $\Theta$  [3]:

$$Z' = Z_\Psi \cos\Theta - Z_\chi \sin\Theta .$$

The best sensitivity to a possible signal from  $Z'$  is achieved through the decay channel,  $Z' \rightarrow \bar{Q}Q$ , where  $Q$  ( $\bar{Q}$ ) stands for a heavy quark (antiquark). The decay  $Z' \rightarrow \bar{Q}Q$  is the most important though not the only production signal possible for  $Z'$ . To search for  $Z'$  at LHC, it is important to know as much as possible about their decay modes in both the standard Drell-Yan (DY)- type sectors and the (super)rare ones. Other channels can provide important information on the  $Z'$  boson couplings. If we go beyond SM, there are several possibilities for some quark bound state resonances  $B \equiv \{\bar{Q}Q\}$  to be produced via the particle interplay accompanied by the Higgs-boson ( $H$ ) emission. A possible extension of the SM adopting a  $Z'$  boson may need more unknown  $h$ -fermions (spin-1/2 heavy exotic quarks) and  $H$  particles to be included. It is known that the  $Z$  boson is not yet an exact mass eigenstate, but turns out to be mixed with  $Z'$ . In the  $Z - Z'$  mixing scheme the mass eigenstates  $Z_1$  and  $Z_2$  are rotated with respect to the basis  $Z$  and  $Z'$

$$\begin{pmatrix} Z_1 \\ Z_2 \end{pmatrix} = \begin{pmatrix} \cos \kappa & \sin \kappa \\ -\sin \kappa & \cos \kappa \end{pmatrix} \begin{pmatrix} Z \\ Z' \end{pmatrix} ,$$

by the mixing angle  $\kappa$

$$\kappa = \arctan \left( \frac{M_Z^2 - M_{Z_1}^2}{M_{Z_2}^2 - M_Z^2} \right)^{1/2}$$

with  $M_{Z_1}$  and  $M_{Z_2}$  being the masses for mass eigenstates  $Z_1$  and  $Z_2$ , respectively.

In this letter, we study a possible extra  $Z_2$  state and its interpretations which have direct implications for NP at LHC. Our interest is in  $Z_2$  production and possible pair production process  $Z_2(W, Z)$  with  $Z_2$  decay into pairs of heavy quarks leading to  $\bar{Q}Q$  and  $\bar{Q}Q(W, Z)$  events at LHC with  $\bar{Q}Q$  invariant mass peaked at the mass up to an order of  $O(0.4 \text{ TeV})$ . If the  $Z_2$  state is heavy enough to produce the  $H$  boson, one can determine the effective coupling of the  $Z_2$ - $H$  interaction. We are to give the estimation of the partial decay widths  $\Gamma$  ratio

$$R(Z_2 \rightarrow H\{\bar{Q}Q\}_{s=1}/\bar{Q}Q) \equiv \frac{\Gamma(Z_2 \rightarrow H\{\bar{Q}Q\}_{s=1})}{\Gamma(Z_2 \rightarrow \bar{Q}Q)} , \quad (1)$$

where  $\{\bar{Q}Q\}_{s=1}$  stands for a spin-1 quark-antiquark bound state.

2. To analyze the  $Z_2$  state effects within the model under consideration, let us concentrate on the  $Z_2$  couplings. Neglecting the interactions of  $Z$  bosons to leptons ("leptophobic" character of  $Z$  bosons) the interactions of mass eigenstates  $Z_i$  ( $i > 1$ ) with heavy quarks are described by the following Lagrangian density:

$$-L_{Z_i Q} = g_Z \sum_{i=1}^{\infty} \sum_Q \bar{Q}(g_{V_i} - g_{A_i} \gamma_5) \gamma^{\mu} Q Z_{i\mu} , \quad (2)$$

where one of the sums runs over all heavy quarks  $Q$ ,  $g_Z$  is presented as the SM coupling  $g/\sqrt{1-s_W^2}$  ( $s_W \equiv \sin \Theta_W$ ),  $Z_{i\mu}$  is understood as the SM  $Z$  boson field while  $Z_j$  with  $j \geq 2$  are additional  $Z$  states in the weak-eigenstate basis. We shall consider the model with one light  $Z_2$  mass eigenstate only. The vector  $g_{V_i}$  and the axial  $g_{A_i}$  couplings ( $i=1,2$ ) in (2) are defined as

$$g_{V_1} = g_V \cos \kappa + g'_V \alpha \sin \kappa , \quad g_{A_1} = g_A \cos \kappa + g'_A \alpha \sin \kappa , \quad (3)$$

$$g_{V_2} = \alpha g'_V \cos \kappa - g_V \sin \kappa , \quad g_{A_2} = \alpha g'_A \cos \kappa - g_A \sin \kappa \quad (4)$$

with

$$g_V = \frac{1}{2} T_{3L} - s_W^2 \cdot e_Q , \quad g_A = \frac{1}{2} T_{3L} ,$$

for  $T_{3L}$  and  $e_Q$  being the third component of the weak isospin and the electric charge, respectively. Both  $g'_V$  and  $g'_A$  in (3)-(4) represent the chiral properties

of the  $Z'$  boson interplay with quarks and the relative strengths of these interactions

$$-L_{Z'Q} = g'_Z \sum_Q \bar{Q}(g'_V - g'_A \gamma_5) \gamma^\mu Q Z'_\mu . \quad (5)$$

For the GUT models, the free parameter  $g'_Z$  in (5) is related to  $\alpha$  in (3)-(4) as  $\alpha \equiv (g'_Z/g_Z) = \sqrt{(5/3)\omega \cdot s_W}$  [4], where  $\omega$  depends on the symmetry breaking pattern and the fermion sector of the model, but is usually taken  $\omega \sim 2/3-1$ . The choice of  $\alpha \simeq 0.62$  provides the equality of both  $g_Z$  and  $g'_Z$  on the scale of the mass of the unification  $M_X \simeq M_{GUT}$  into  $E_6$ . Neglecting some differences in the renormalization group evolution of both  $g_Z$  and  $g'_Z$ , one can deal with  $\alpha$  at the energies  $\sim M_{Z'} \sim M_{Z_2} \sim O(1 \text{ TeV})$ .

Suppose that the  $Z_2$  state could be produced at LHC via  $\bar{Q}Q \rightarrow Z_2$  subprocess, and in the narrow  $Z_2$  width approximation the cross section

$$\sigma(\bar{Q}Q \rightarrow Z_2) = K(M_{Z_2}) \frac{2\pi G_F M_{Z_1}^2}{3\sqrt{2}} (g_{V_2}^2 + g_{A_2}^2) \delta(s - M_{Z_2})$$

is both  $M_{Z_2}$ - and  $\kappa$ - dependent. Here,  $G_F$  is the Fermi constant and  $K$  factor reflects the higher order QCD process [5]

$$K(M_{Z_2}) = 1 + \frac{\alpha_s(M_{Z_2}^2)}{2\pi} \frac{4}{3} \left( 1 + \frac{4}{3} \pi^2 \right) .$$

Note that two-loop  $\alpha_s(M_{Z_2}^2) \sim 0.1$  for  $\Lambda_{QCD} = 200 \text{ MeV}$  at  $M_{Z_2} < 2m_t$  (5 flavors) and  $M_{Z_2} > 2m_t$  (6 flavors) for  $m_t$  being the top quark mass [2].

The partial width for  $Z_2$  decays into quarks is determined by the couplings  $g_{V_2}$  and  $g_{A_2}$  (4), namely (the number of colors  $N_c=3$  is taken into account)

$$\begin{aligned} \Gamma(Z_2 \rightarrow \bar{Q}Q) &= \frac{2 G_F M_Z^2}{\sqrt{2}\pi} C(M_{Z_2}^2) M_{Z_2} \\ &\times (1 - 4r_q)^{1/2} \left[ g_{V_2}^2 (1 + 2r_q) + g_{A_2}^2 (1 - 4r_q) \right] . \end{aligned} \quad (6)$$

Here,  $r_q \equiv m^2/M_{Z_2}^2$ ,  $M_Z$  and  $m$  are the masses of the  $Z$  boson and a quark, respectively, while the  $C$  factor is defined by the running strong coupling constant  $\alpha_s$

$$C(\mu^2) = 1 + \frac{\alpha_s(\mu^2)}{\pi} + 1.409 \frac{\alpha_s^2(\mu^2)}{\pi^2} - 12.77 \frac{\alpha_s^3(\mu^2)}{\pi^3}$$

with an arbitrary scale  $\mu$ . The interactions of the  $Z_2$  state with quarks are expressed in terms of three parameters  $x$ ,  $y^u$  and  $y^d$  [1], where labels  $u$  and  $d$  mean the up- and down-type of quarks

$$2g_{V_2}^u = x + y^u \quad , \quad -2g_{A_2}^u = -x + y^u \quad , \\ 2g_{V_2}^d = x + y^d \quad , \quad -2g_{A_2}^d = -x + y^d \quad ,$$

3. The  $\{\bar{Q}Q\}_{s=1}$  bound state with the 4-momentum  $Q_\mu$  and the mass  $m_B$  may be produced in the  $Z_2$  state decay via the  $H$  boson emission with the 4-momentum  $k_\mu$  in a heavy quark-loop scheme. The decay amplitude is written as

$$A(k, Q) = \int d_4q \text{Tr} \left\{ \Gamma_Q^+(q) \cdot \sum_{i=1}^3 T_i(q, k; Q) \right\} , \quad (7)$$

where  $\Gamma_Q(q_\mu)$  is the spin-1 quark bound state vertex function depending on the relative momentum  $q_\mu$  of  $\bar{Q}$  and  $Q$ , while  $T_i$  are the rest of the total matrix element. In fact,  $T_i$  in (7) carry the dependence of interplay of  $H$  to heavy quarks ( $i=1,2$ ) and  $Z_2$  state to  $H$  boson ( $i=3$ ) via the couplings  $g_H = m/\langle H \rangle_0$  and  $g_{Z_2 H} = 2M_{Z_2}^2/\langle H \rangle_0$ , respectively, where  $\langle H \rangle_0$  stands for the vacuum expectation value of the singlet field  $H$ . Generally,  $\Gamma_Q(q_\mu)$  is constructed [6] in terms of quark  $u(Q_\mu)$  and antiquark  $v(\bar{Q}_\mu)$  spinors in a given spin configuration accompanied by the covariant confinement-type wave function  $\phi_Q(q^2; \beta)$  (in  $\Re(S_4)$ ) containing the model parameter  $\beta$  [7]

$$\Gamma_Q(q_\mu) = \bar{u}(Q_\mu) \frac{\delta_i^j}{\sqrt{3}} U_{\alpha\beta} \phi_Q(q^2; \beta) v(\bar{Q}_\mu) . \quad (8)$$

Here, the second rank symmetric spinors  $U_{\alpha\beta}$  obey the standard Bargman-Wigner equations [8]  $(\mathcal{Q} - m_B)_\alpha^{\alpha'} U_{\alpha'\beta} = 0$ .

The decay width of  $Z_2 \rightarrow H\{\bar{Q}Q\}_{s=1}$  is given by

$$\Gamma(Z_2 \rightarrow H\{\bar{Q}Q\}_{s=1}) = \frac{g_Z^2 g_{V_2}^2 M_{Z_2}^3 N_C \cos^2 \vartheta x_\beta^2 \sqrt{\lambda(1, x_H, x_B)}}{\pi^3 (1 - x_B) \langle H \rangle_0^2} \\ \cdot (1 - 6x_\beta/x_B) \times \left\{ \frac{1}{4d_0} \left[ \frac{1}{3} (1 - x_H) \left( 1 - 5 \frac{x_\beta}{d_0} \right) + \frac{5}{12} x_B \left( 1 + \frac{8x_\beta}{5d_0} \right) + \frac{1}{4} x_B \right. \right. \\ \left. \left. - 5x_\beta - \frac{1}{3} (x_H - x_B)^2 \left( 1 + 4 \frac{x_\beta}{d_0} \right) \right] + \frac{1 - 6x_\beta/x_B}{1 - x_B} \right\} , \quad (9)$$

where  $r_B \simeq (2m/M_{Z_2})^2$ ,  $x_H \equiv (m_H/M_{Z_2})^2$   $x_\beta \equiv \beta/M_{Z_2}^2$ ,  $d_0 \simeq \frac{1}{2}(1+x_H-x_B)$ ,  $\cos\vartheta \equiv (\epsilon \cdot \epsilon_{Z_2})$  for  $\epsilon^\mu$  and  $\epsilon_{Z_2}^\mu$  being the polarization four-vectors of  $B$  and  $Z_2$  state, respectively.

The total relative width  $R(Z_2 \rightarrow H\{\bar{b}b\}_{s=1}/\bar{b}b)$  (1), derived from Eqs. (6) and (9) in the case when  $B$  is composed of  $\bar{b}b$  but for the  $\bar{b}b$  DY-type normalization, is presented in Table 1 as a function of the  $H$  boson mass  $m_H$  via the ratio  $x_H$ .

Table 1 The values of  $R(Z_2 \rightarrow H\{\bar{b}b\}_{s=1}/\bar{b}b) \times 10^{10}$  for various embedding scales  $M_{Z_2}$  and Higgs boson masses  $m_H$  via the ratio  $x_H = (m_H/M_{Z_2})^2$ .

$M_{Z_2}$ (TeV)	$x_H$					
	0	0.2	0.4	0.6	0.8	0.9
0.2	2.60	2.00	1.40	0.90	0.43	0.21
0.3	1.20	0.90	0.62	0.40	0.19	0.09
0.5	0.42	0.32	0.23	0.15	0.07	0.03
0.7	0.21	0.16	0.11	0.07	0.04	0.02

To be definite we have considered four values of  $M_{Z_2}=0.2$ , 0.3, 0.5 and 0.7 TeV. As can be seen, the distribution is very steeply peaked towards low  $H$  boson masses and drops to zero at high mass end. In fact, the results are valid for any masses by simply rescaling the ratios  $x_{H,B,\beta}$ . To be understood precisely, one has to note the following: firstly, the  $B$  state is treated relativistically (see (8)) and in the zero binding energy  $m_B \simeq 2m$ ; secondly, gluon corrections to the process have not been included. For a heavy  $B$  state such as  $\{\bar{b}b\}_{s=1}$  or  $\{\bar{t}t\}_{s=1}$ , both of these approximations should be accepted. For a light spin-1  $B$  state (heavier Higgs boson), the results can only be taken as a guide of an order of magnitude of the rates.

The only interesting point has been omitted from our consideration, namely, the  $Z'$ -decays via spin-1/2 exotic quarks ( $h$ ) with Higgs boson emission. The exotic quarkonium  $\{\bar{h}h\}$  and open flavor  $\{\bar{Q}h\}$  bound states of the exotic  $h$ -quark production are under consideration, while they have gained attention in many papers. These bound states, eg.,  $\{\bar{h}Q\}$ , can be formed since the spectator decays of a heavy quark constituent  $h \rightarrow Q + H$  or  $h \rightarrow Q + W(Z)$  are expected to be suppressed due to small mixing of exotic-SM constituents. The model presented in this letter is an instructive one to study and discover extra gauge bosons at LHC and NLC .

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